

$B_s^0 \rightarrow D_s^{(*)-} D_s^{(*)+}$ branching fractions
and determination the $B_s^0 - \bar{B}_s^0$ width
difference at Belle

Sevda Esen
University of Cincinnati



September 18, 2012



Standard Model:

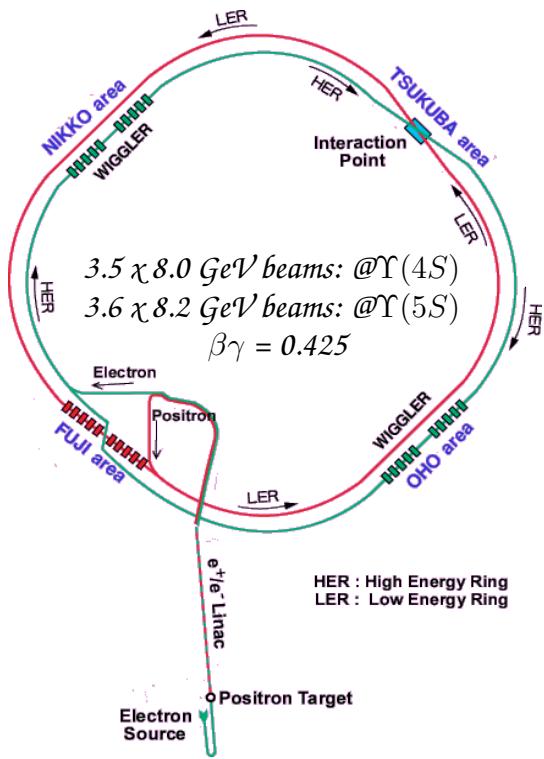
- describes fundamental particles
 - ▷ the six type ("flavors") of quarks
 u, d, s, c, b, t
 - ▷ the six type of leptons
 $e, \mu, \tau, \nu_e, \nu_\mu, \nu_\tau$
- explains their interactions via gauge bosons
 $\gamma, W, Z, \text{gluon}$

Heavy Flavor Physics:

- investigates interactions that differ among flavors
- looks for properties of heavy flavor hadrons: b, c, τ
- significant amount of data from:

Belle, BaBar, CDF, D0, CMS, ATLAS, and LHCb

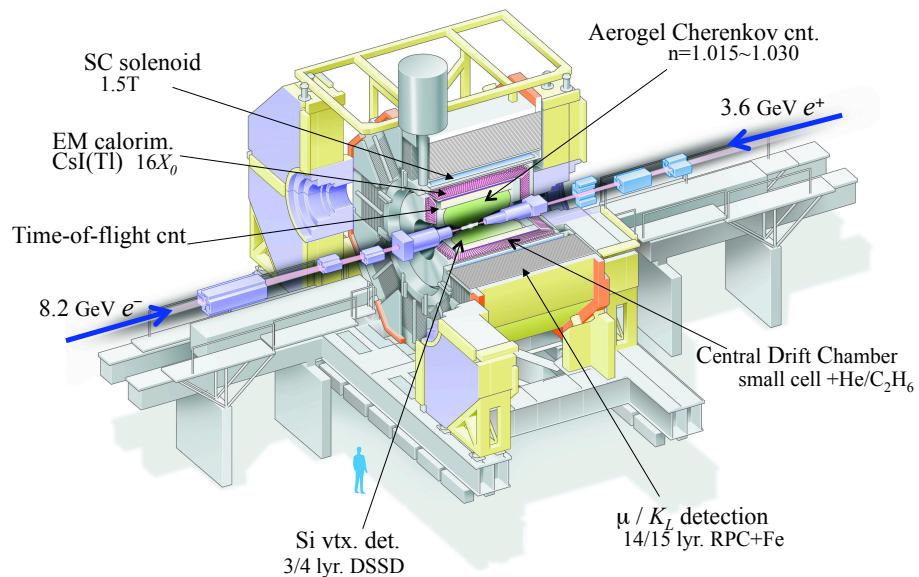
B-factories → dedicated to B mesons



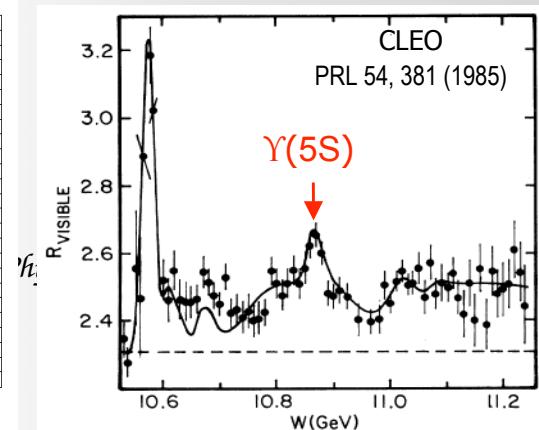
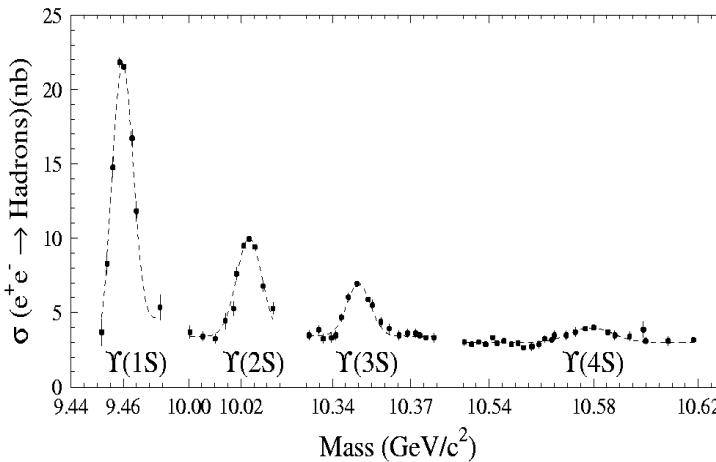
Primary goal:

study CP violation in B sector

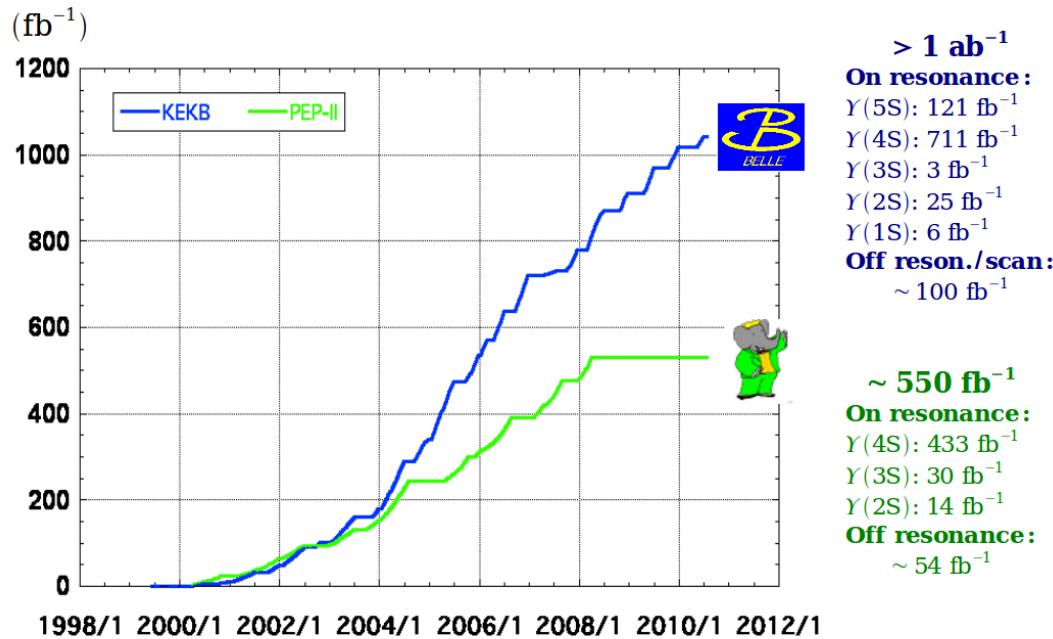
$711 \text{ fb}^{-1} = 770M B$ events recorded at $\Upsilon(4S)$



Υ Resonances ($b\bar{b}$ bound states)

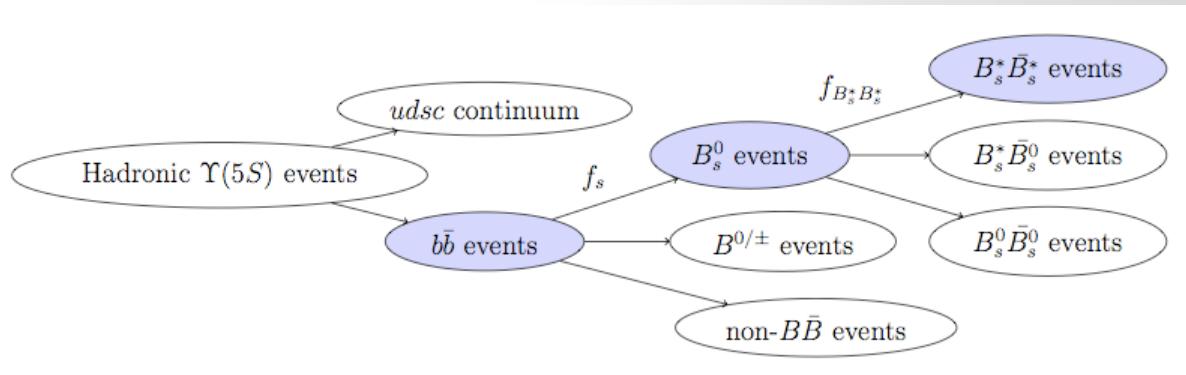


- ✓ The Υ resonances are bound states of $b\bar{b}$ quarks.
- ✓ The lightest Υ resonance producing $B\bar{B}$ pair is $\Upsilon(4S)$
- ✓ The $\Upsilon(5S)$ resonance is heavy enough to produce $B_s^{(*)}\bar{B}_s^{(*)}$ pairs
- ✓ A large background due to light-quark pair production (u, d, s or c quark pairs)



- World luminosity record $L = 2.11 \times 10^{34} \text{ cm}^{-1} \text{s}^{-1}$
- Data taken at $\Upsilon(4S)$, below $\Upsilon(4S)$ (continuum), at $\Upsilon(5S)$, and above $\Upsilon(5S)$ (scan)
- 121.4 fb^{-1} data, corresponding to 7.11 million $B_s^{(*)} B_s^{(*)}$ pairs, used for this analysis

$B_s \rightarrow D_s^{(*)+} D_s^{(*)-}$ Branching Fraction



The total number of $B_s \bar{B}_s$ pairs: $N_{B_s \bar{B}_s} = \mathcal{L} \times \sigma_{b\bar{b}}^{\Upsilon(5S)} \times f_s$

✓ Luminosity: $\mathcal{L} = 121.4 \text{ fb}^{-1}$

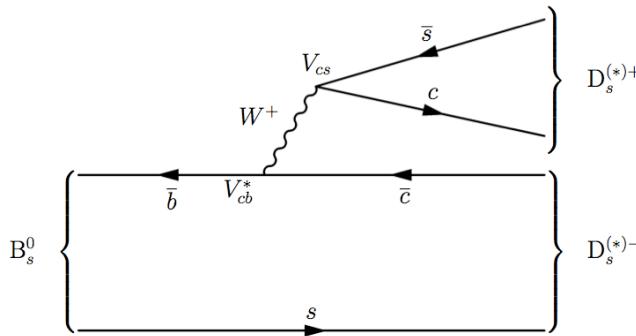
✓ $e^+e^- \rightarrow b\bar{b}$ cross section at $\Upsilon(5S)$ energy: $\sigma_{b\bar{b}}^{\Upsilon(5S)} = 0.340 \pm 0.016 \text{ nb}$

✓ Fraction of the $\Upsilon(5S)$ decays producing B_s^0 mesons: $f_s = (17.1 \pm 3.0)\%$

$$\mathcal{B}(\Upsilon(5S) \rightarrow D_s X)/2 = f_s \times \mathcal{B}(B_s^0 \rightarrow D_s X) + (1 - f_s) \times \mathcal{B}(B \rightarrow D_s X)$$

$$\text{✓ } N_{B_s^{(*)} B_s^{(*)}} = (7.11 \pm 1.30) \times 10^6$$

$B_s^0 \rightarrow D_s^{(*)+} D_s^{(*)-}$ Decays



- ▷ CKM -favored and flavor-neutral
- ▷ Dominant \mathcal{CP} -even final states
- ▷ Two heavy D_s in the final state

- $D_s^+ D_s^-$ pure \mathcal{CP} -even
- $D_s^{*\pm} D_s^\mp$ should be \mathcal{CP} -even
for negligible CP violation in heavy quark limit *Phys. Lett. B* 316, 567 (1993)
- $D_s^{*+} D_s^{*-}$ predominantly \mathcal{CP} -even:
expected CP -odd fraction is small *Phys. Rev. D* 42, 3732 (1990)
- possible access to $\Delta\Gamma_s$?

- ▷ Exclusively reconstruct B_s^0 decays to $D_s^+ D_s^-$, $D_s^{*\pm} D_s^\mp$ and $D_s^{*+} D_s^{*-}$
 - $D_s^+ \rightarrow \phi\pi^+, K_S K^+, K^{*0} K^+, \phi\rho^+, K^{*+} K_S, K^{*+} K^{*0}$
 - Charged tracks required to originate from near e^+e^- interaction point
 - Mass cut on intermediate resonances and D_s^\pm
- $D_s^{*\pm} \rightarrow D_s^\pm \gamma$ with $|\Delta M_{D_s^* - D_s} - \Delta M^{PDG}| < 12 MeV$
- ▷ Background level is low
- ▷ Observables: the energy difference and the beam energy constrained mass
 - $\Delta E = E_{B_s^0} - E^*$ within $[-0.15, 0.1] GeV$
 - $M_{bc} = \sqrt{E^{*2} - p_{B_s^0}^2}$ within $[5.25, 5.45] GeV/c^2$

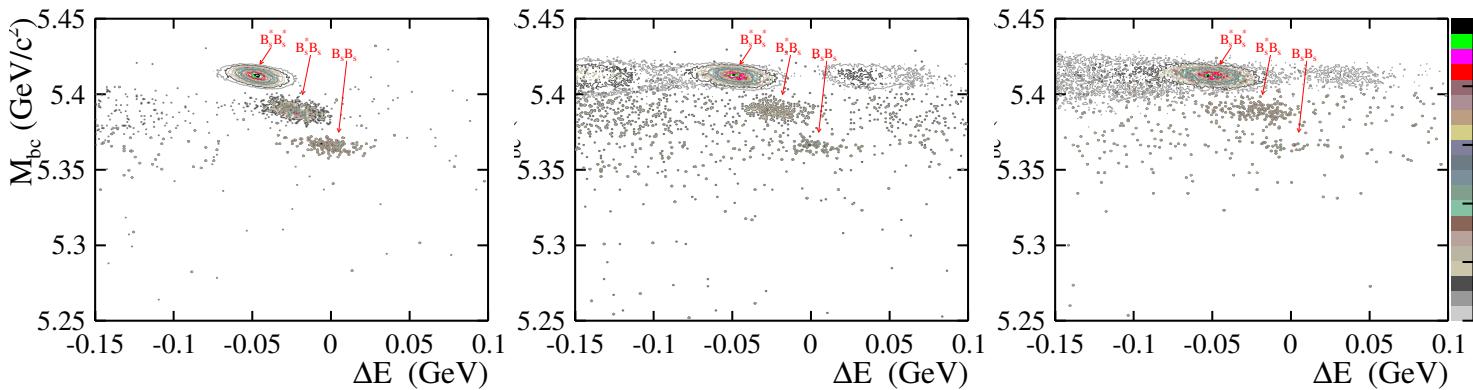
where

E_{beam}^* : the center of mass (CM) beam energy

$E_{B_s^0}$ and $p_{B_s^0}$: the energy and momentum of B_s^0 in the Υ ($5S$) CM rest frame.

✓ $\Upsilon(5S)$ decays through: $B_s^* \bar{B}_s^*$, $B_s^* \bar{B}_s$, $B_s \bar{B}_s$ with $f_{B_s^* \bar{B}_s^*} = 87\%$

- B_s^* always decays to $B_s \gamma$
- We don't reconstruct $\gamma \Rightarrow$ shifted ΔE and M_{bc}



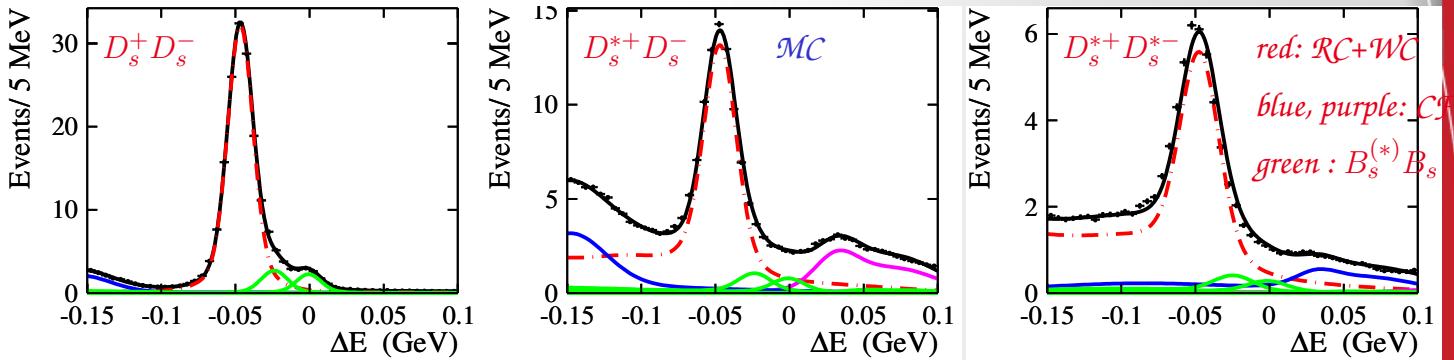
✓ cross contamination between modes

- true D_s^{*+} decay, D_s^+ combined with a random photon \rightarrow WC
- true D_s^+ decay, combined with a random photon \rightarrow CFup
- true D_s^{*+} decay, lost its photon \rightarrow CFdown
- true D_s^{*+} or D_s^+ decay \rightarrow RC

need to pick one, the best

Best Candidate Selection

✓ simultaneous fit of three modes to account for large cross-feeds between signal modes



✓ Relative fractions of signal components

B_s^0 Generated Modes	\mathcal{RC}	\mathcal{WC}	$\mathcal{CF}\ I$	$\mathcal{CF}\ II$
$D_s^+ D_s^-$	76.1	6.0 <i>fixed</i>	17.1 ($D_s^{*\pm} D_s^\mp$)	0.8 ($D_s^{*+} D_s^{*-}$)
$D_s^{*\pm} D_s^\mp$	44.4	38.5 <i>fixed</i>	8.2 ($D_s^+ D_s^-$) <i>fixed</i>	8.9 ($D_s^{*+} D_s^{*-}$)
$D_s^{*+} D_s^{*-}$	31.8	37.6 <i>fixed</i>	2.0 ($D_s^+ D_s^-$) <i>fixed</i>	28.6 ($D_s^{*\pm} D_s^\mp$) <i>fixed</i>

✓ one candidate per event selected with minimum χ^2 (\mathcal{MC} : correct 75% of time)

$$\chi^2 = \frac{1}{2+N} \left\{ \begin{array}{l} \sum_{i=1}^2 \left[(\widetilde{M}_{D_s^i} - M_{D_s})/\sigma_M \right]^2 + \\ \sum_{i=1}^N \left[(\widetilde{\Delta M}_{D_s^{*i}-D_s^i} - \Delta M_{D_s^{*i}-D_s})/\sigma_{\Delta M} \right]^2 \end{array} \right\}$$

- ▷ Continuum - $ud\bar{s}c$ events
 - small amount
 - 93% rejected based on event topology
- ▷ $\Upsilon(5S) \rightarrow B\bar{B}X \rightarrow D_s Y$
 - dominant source
 - can not be removed
 - not peaking in fit variables
- ▷ Exited D_s states
 - consider $D_{sJ}(2317)D_s$, $D_{sJ}(2317)D_s^*$ and $D_{sJ}(2457)D_s$ modes
 - also $D_s D_s \pi^0$ mode
 - small branching fractions expected \Rightarrow not a significant source

- ✓ 2D extended unbinned ML fit to ΔE and M_{bc} to obtain the signal yields in three signal modes.
- ✓ For each event (i), the contribution (j) from the signal and background is modeled independently.
- ✓ The likelihood function for each signal mode is defined as

$$\mathcal{L} = \frac{e^{-\sum Y_j}}{N!} \prod_{i=1}^N \sum_j Y_j \mathcal{P}_j^i, \quad (1)$$

- ✓ The combined likelihood to be maximized

$$\mathcal{L} = \mathcal{L}_{D_s^+ D_s^-} \cdot \mathcal{L}_{D_s^{*\pm} D_s^\mp} \cdot \mathcal{L}_{D_s^{*+} D_s^{*-}}. \quad (2)$$

- ✓ The yields of the RC components from $B_s^* B_s^*$ production are the common parameters.

- try the simultaneous fit with more statistics
- data/MC calibration factors for signal PDFs
- obtain the systematics errors for
 - continuum suppression, best candidate selection

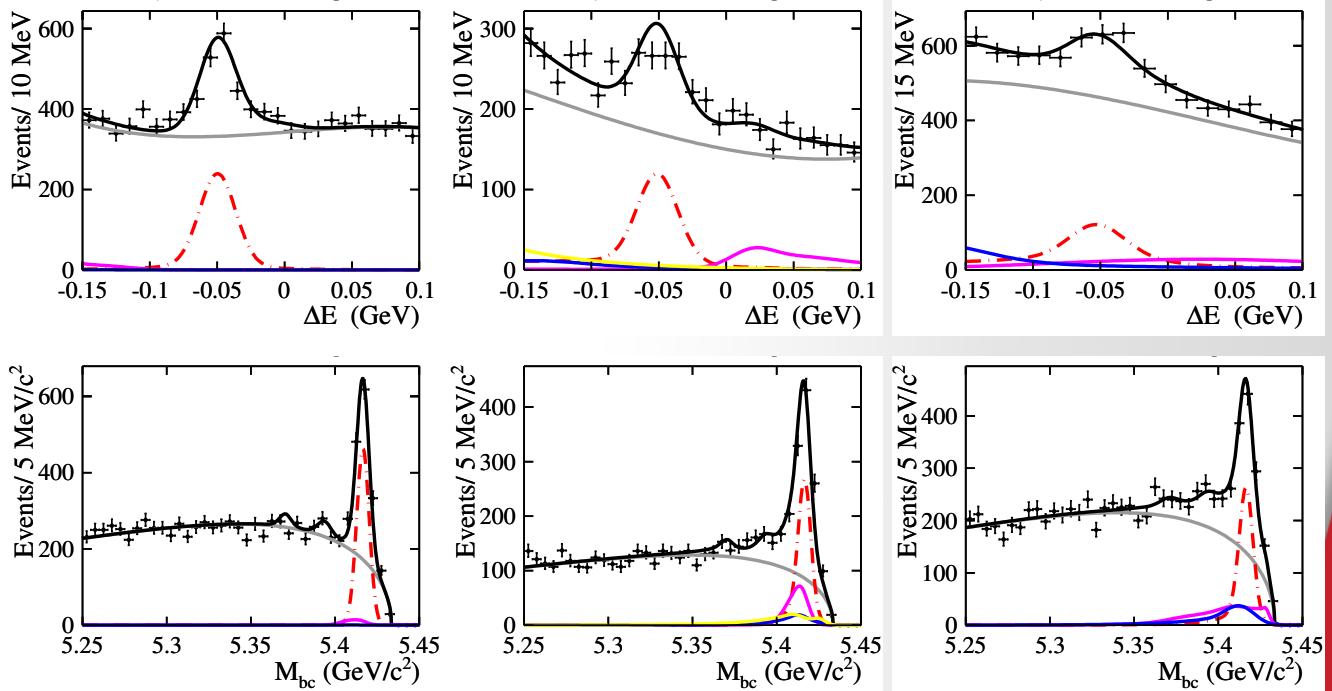
Two samples:

$B_s \rightarrow D_s^{(*)-} h^+$ with $\Upsilon(5S)$ data

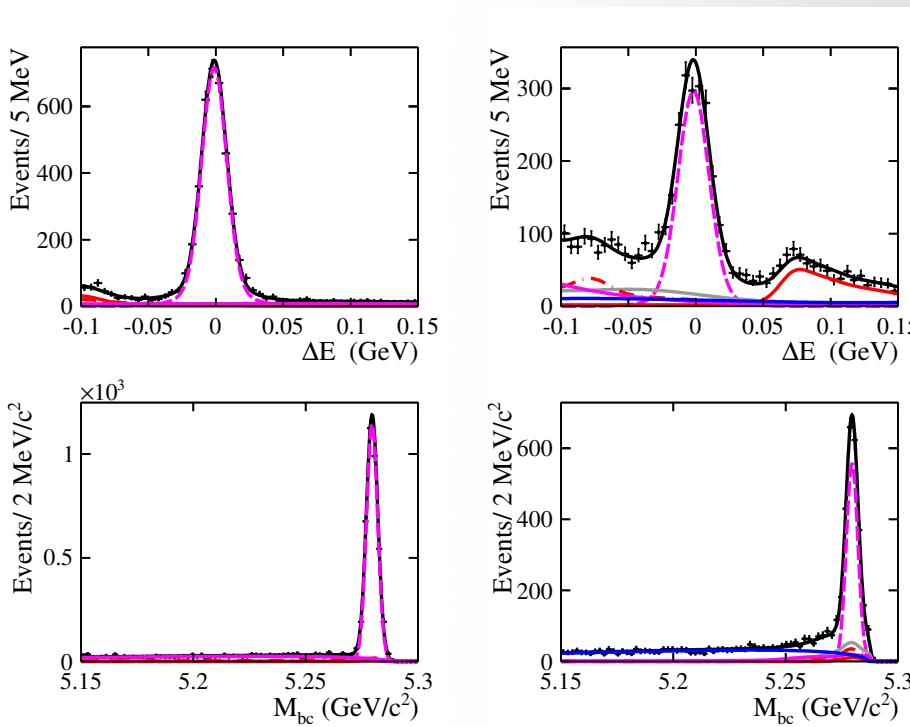
- Three decay modes: $D_s^- \pi^+$, $D_s^{*-} \pi^+$ and $D_s^- \rho^+$
- Same event selection
- Slightly modified best candidate selection

$B^0 \rightarrow D^{(*)+} D^-$ with $\Upsilon(4S)$ data

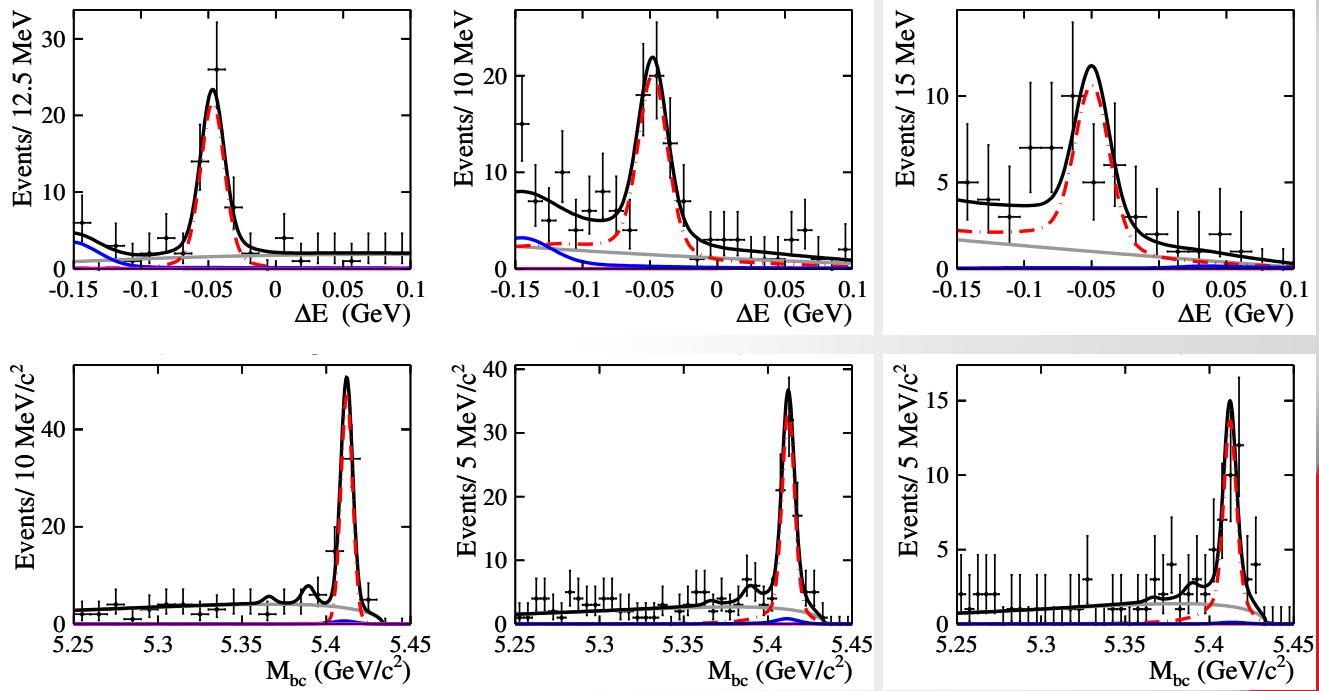
- Two decay modes: $D_s^+ D^-$ and $D_s^{*+} D^-$ where $D^- \rightarrow K^+ \pi^- \pi^-$
- Similar kinematics
- Same event selection



<i>Mode</i>	$B(B_s \rightarrow D_s^- \pi^+) (10^{-3})$	$BF(B_s \rightarrow D_s^{*-} \pi^+) (10^{-3})$	$BF(B_s \rightarrow D_s^- \rho^+) (10^{-3})$
<i>This study</i>	3.42 ± 0.13	3.48 ± 0.02	8.53 ± 0.51
<i>PDG</i>	3.2 ± 0.5	2.1 ± 0.6	7.4 ± 1.8

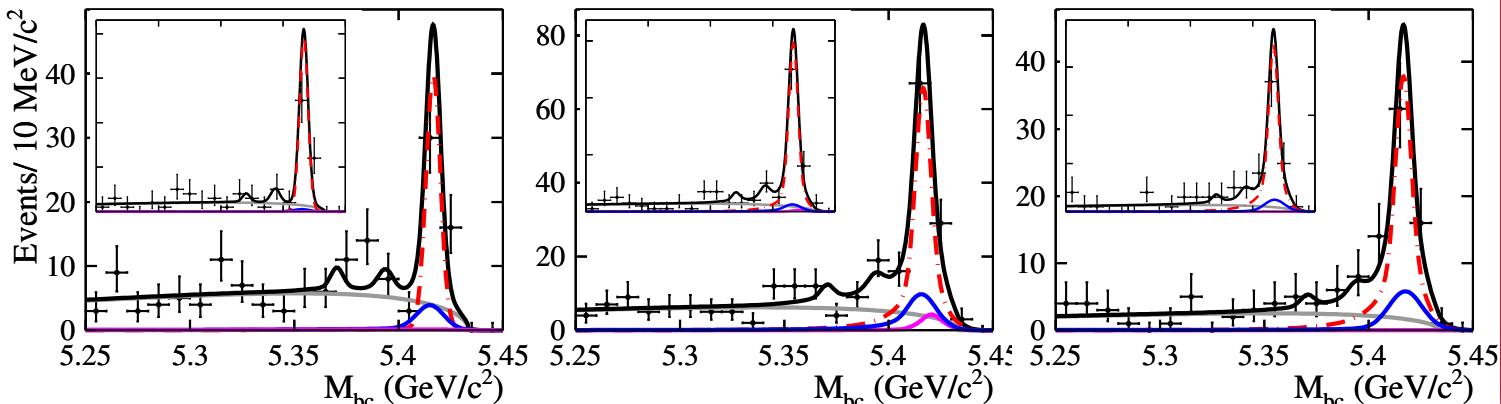


	$B(B^0 \rightarrow D_s^- D^+) (10^{-3})$	$BF(B^0 \rightarrow D_s^{*-} D^+) (10^{-3})$
<i>with BCS /event</i>	6.76 ± 0.12	6.65 ± 0.17
<i>without BCS /event</i>	7.13 ± 0.11	6.75 ± 0.18
<i>PDG</i>	7.2 ± 0.8	7.4 ± 1.6



	<i>input</i>	0	1	2	3	4	5
$D_s D_s$	0.86	$0.68^{+0.11}_{-0.10}$	$0.71^{+0.11}_{-0.10}$	$0.84^{+0.12}_{-0.11}$	$1.10^{+0.13}_{-0.12}$	$0.99^{+0.13}_{-0.12}$	$1.00^{+0.13}_{-0.12}$
$D_s^* D_s$	1.89	$1.84^{+0.23}_{-0.21}$	$1.70^{+0.22}_{-0.20}$	$2.05^{+0.24}_{-0.22}$	$1.77^{+0.22}_{-0.21}$	$1.70^{+0.22}_{-0.21}$	$2.14^{+0.25}_{-0.23}$
$D_s^* D_s^*$	1.97	$1.47^{+0.29}_{-0.27}$	$1.85^{+0.29}_{-0.26}$	$1.66^{+0.27}_{-0.25}$	$2.42^{+0.31}_{-0.29}$	$1.26^{+0.26}_{-0.24}$	$1.90^{+0.31}_{-0.29}$

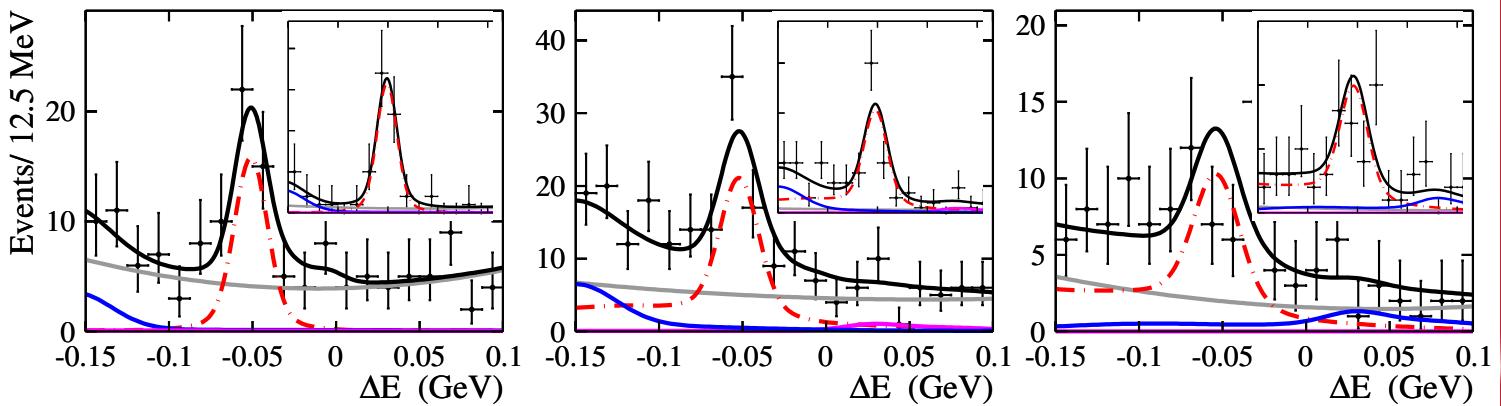
signal region: $\Delta E[-0.1, 0.0]$ and $M_{bc}[5.4, 5.43]$ (small figures)



$$D_s^+ D_s^- = 33.1^{+6.0}_{-5.4}$$

$$D_s^{*+} D_s^- = 44.5^{+5.8}_{-5.5}$$

$$D_s^{*+} D_s^{*-} = 24.4^{+4.1}_{-3.8}$$



Systematic Errors (%)

Source	$D_s^+ D_s^-$		$D_s^* D_s$		$D_s^{*+} D_s^{*-}$	
	$+\sigma$	$-\sigma$	$+\sigma$	$-\sigma$	$+\sigma$	$-\sigma$
Signal PDF Shape	2.7	2.2	2.2	2.4	5.1	3.8
Background PDF Shape	1.5	1.3	1.3	1.4	2.9	2.8
WC + CF fraction	0.5	0.5	4.7	4.5	11.0	9.7
\mathcal{R} requirement ($q\bar{q}$) suppr.	3.1	0.0	0.0	2.7	0.0	2.1
Best candidate selection	5.5	0.0	1.5	0.0	1.5	0.0
K^\pm Identification	7.0	7.0	7.0	7.0	7.0	7.0
K_s Reconstruction	1.1	1.1	1.1	1.1	1.1	1.1
π^0 Reconstruction	1.1	1.1	1.1	1.1	1.1	1.1
γ	-	-	3.8	3.8	7.6	7.6
Tracking	2.2	2.2	2.2	2.2	2.2	2.2
Polarization	0.0	0.0	0.8	2.4	0.4	0.2
\mathcal{MC} statistics for ε	0.2	0.2	0.4	0.4	0.5	0.5
$D_s^{(*)}$ \mathcal{BF} 's	8.6	8.6	8.6	8.6	8.7	8.7
$N_{B_s^{(*)} B_s^{(*)}}$				18.3		
$f_{B_s^* \overline{B}_s^*}$				2.0		
Total	22.7	21.8	22.7	22.9	26.2	25.5

"External errors

Mode	$\mathcal{Y}(\text{events})$	$\varepsilon_{MC} (\times 10^{-4})$	$\mathcal{B} (\%)$	S
$D_s^+ D_s^-$	$33.1^{+6.0}_{-5.4}$	4.72	$0.58^{+0.11}_{-0.09} \pm 0.13$	11.6
$D_s^{*+} D_s^- + D_s^{*-} D_s^+$	$44.5^{+5.8}_{-5.5}$	2.08	$1.8 \pm 0.2 \pm 0.4$	13.3
$D_s^{*+} D_s^{*-}$	$24.4^{+4.1}_{-3.8}$	1.01	$2.0 \pm 0.3 \pm 0.5$	8.6
<i>Sum</i>	$102.0^{+9.3}_{-8.6}$		$4.3 \pm 0.4 \pm 1.0$	

Branching Fraction

$$\mathcal{B} = \frac{Y}{2 \times N_{B_s^* B_s^*} \times \varepsilon_{MC} \times \varepsilon_{PID}}$$

Significance

$$S = \sqrt{-2 \ln(\mathcal{L}_0 / \mathcal{L}_{max})}$$

- ✓ *Belle measured: three decay modes exclusively*
- ✓ *CDF measured: B_s^0 production rate times $B_s^0 \rightarrow D_s^{(*)+} D_s^{(*)-}$ branching ratios relative to the normalization mode $B^0 \rightarrow D_s^+ D^-$*
- ✓ *The D0 measured: $B_s^0 \rightarrow D_s^{(*)+} D_s^{(*)-}$ via an inclusive analysis*

Mode	<i>Belle</i> ⁽¹⁾ (10^{-2})	<i>CDF</i> ⁽²⁾ (10^{-2})	<i>D0</i> ⁽³⁾ (10^{-2})
$D_s^+ D_s^-$	$0.58_{-0.09}^{+0.11} \pm 0.13$	$0.49 \pm 0.06 \pm 0.05 \pm 0.08$	
$D_s^{*\pm} D_s^{\mp}$	$1.8 \pm 0.2 \pm 0.4$	$1.13 \pm 0.12 \pm 0.09 \pm 0.19$	
$D_s^{*+} D_s^{*-}$	$2.0 \pm 0.3 \pm 0.5$	$1.75 \pm 0.19 \pm 0.17 \pm 0.28$	
$D_s^{(*)+} D_s^{(*)-}$	$4.3 \pm 0.4 \pm 1.0$	$3.38 \pm 0.25 \pm 0.30 \pm 0.56$	$3.5 \pm 1.0 \pm 1.1$

⁽¹⁾ S. Esen et al. (Belle Collaboration), arXiv:1208.0323 (to be published in PRD(RC))

⁽²⁾ T. Aaltonen et al., (CDF Collaboration) PRD 85 (2012), 072002

⁽³⁾ V.M.. Abazov et al. (D0 Collaboration), PRL 102 (2009), 091801

$B_s - \bar{B}_s$ Width Difference

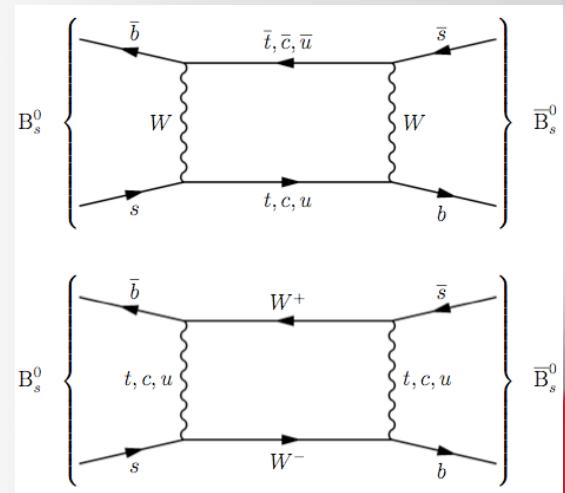
Time evolution of the $B_s^0 - \bar{B}_s^0$ system:

$$i \frac{d}{dt} \begin{pmatrix} B_s^0 \\ \bar{B}_s^0 \end{pmatrix} = \begin{pmatrix} M_s - i\Gamma_s/2 & M_{12} - i\Gamma_{12}/2 \\ M_{12}^* - i\Gamma_{12}^*/2 & M_s - i\Gamma_s/2 \end{pmatrix} \begin{pmatrix} B_s^0 \\ \bar{B}_s^0 \end{pmatrix}$$

The mass eigenstates:

$$\begin{aligned} |B_{sH}^0\rangle &= p |B_s^0\rangle + q |\bar{B}_s^0\rangle \\ |B_{sL}^0\rangle &= p |B_s^0\rangle - q |\bar{B}_s^0\rangle \end{aligned}$$

with $|p|^2 + |q|^2 = 1$.



Define:

$\Delta m_s = M_H - M_L > 0$ and $\Delta\Gamma_s = \Gamma_L - \Gamma_H (> 0 \text{ PRD 108, 241801 (2012)})$

World averages (\mathcal{HFAg})

$$\Delta m_s = 17.69 \pm 0.08 \text{ ps}^{-1} \text{ and } 1/\Gamma_s = 1.495 \pm 0.015 \text{ ps}$$

Observation of $\Gamma_s \ll \Delta m_s$ implies

$$\Gamma_{12} \ll M_{12},$$

and thus, to a good approximation:

$$\begin{aligned}\Delta m_s &\approx 2|M_{12}|, \\ \Delta\Gamma_s &\approx 2|\Gamma_{12}| \cos\phi_s,\end{aligned}$$

with the CP violating phase

$$\phi_s = \arg\left(-\frac{M_{12}}{\Gamma_{12}}\right)$$

which is predicted to be small in the SM. *Phys. Rev. D*
84, 033005 (2011)

- Δm_s :
sensitive to new physics
well measured
consistent w/ SM

ϕ_s :
very sensitive to NP

$\Delta\Gamma_s$:
moderately sensitive to NP
not well known

- Neglecting CP violation, the heavy and light mass eigenstates have definite CP parity. For $\phi_s = 0$, $\Delta\Gamma_s = \Delta\Gamma_s^{CP}$
- The decay channels common to B_s^0 and \bar{B}_s^0 mesons contribute to Γ_{12} and thus determine $\Delta\Gamma_s$.
- CKM favored $b \rightarrow c\bar{c}s$ transition dominates such modes
- CP specific or flavor specific modes can be used to extract $\Delta\Gamma_s$ *Phys. Rev. D 52, 3048 (1995); Phys. Lett. B 316, 567 (1993)*
- Best probed with $B_s \rightarrow J/\psi\phi$ angular analysis
- $B_s^0 \rightarrow D_s^{(*)+}D_s^{*-}$ constitute significant fraction of $b \rightarrow c\bar{c}s$
 - predominantly CP -even.
 - large branching fraction
 - non-negligible theoretical uncertainties *Phys. Rev. D 84, 074037 (2011)*

✓ In the heavy quark limit, while $(m_b - 2m_c) \rightarrow 0$ and $N_c \rightarrow \infty$

✓ $b \rightarrow c\bar{c}s$ processes contribute constructively to $\Delta\Gamma_s$

✓ $\Gamma[B_s^0(CP+) \rightarrow D_s^{(*)-} D_s^{(*)+}]$ saturates $\Delta\Gamma_s^{CP}$

✓ assuming negligible \mathcal{CP} violation, we can estimate $\Delta\Gamma_s/\Gamma_s$

$$\frac{\Delta\Gamma_s}{\Gamma_s} = \frac{2\mathcal{B}(B_s^0 \rightarrow D_s^{(*)-} D_s^{(*)+})}{1 - \mathcal{B}(B_s^0 \rightarrow D_s^{(*)-} D_s^{(*)+})}$$

Aleksan et. al., *PLB* 316, 567 (1993), Dunietz et. al. , *PRD* 63, 114015 (2001)

*some
theoretical
uncertainty*

✓✓ 3-body $D_s^{(*)} D_{(s)}^{(*)} X$ and $D_{sJ} D_s$ final states are not included

✓✓ $D_s^{*+} D_s^{*-}$ mode is expected to have a small \mathcal{CP} -odd component

	$\mathcal{Y}(\text{events})$	$\mathcal{B} (\%)$
$B_s \rightarrow D_s^{(*)} D_s^{(*)}$	$102.0^{+9.3}_{-8.6}$	$4.3 \pm 0.4 \pm 1.0$
$\Delta\Gamma_s/\Gamma_s$	$(9.0 \pm 0.9 \pm 2.2) \%$	

$$\Delta\Gamma_s/\Gamma_s = 2\mathcal{B}/(1 - \mathcal{B})$$

$$\text{using } \Gamma_s = 1.463 \pm 0.030 \text{ ps}^{-1} \Rightarrow \Delta\Gamma_s = 0.062 \pm 0.016 \text{ ps}^{-1}$$

▷ Theoretical Estimations:

$$\Delta\Gamma_s/\Gamma_s = (13.3 \pm 3.2)\% \text{ arXiv:hep-ph/1102.4274}$$

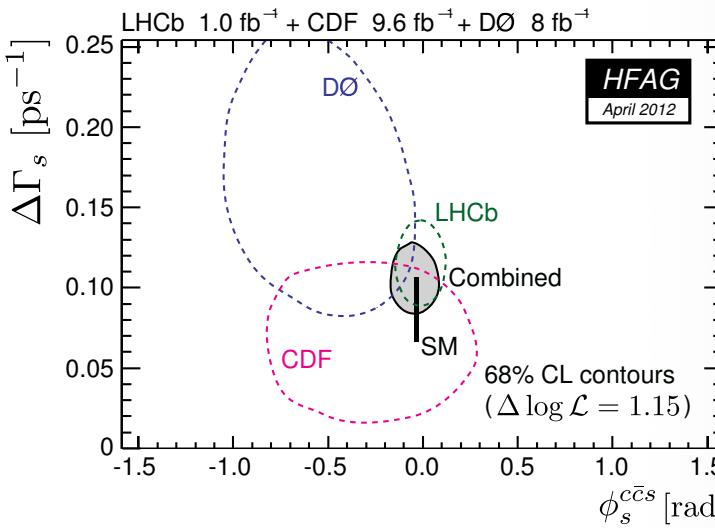
$$\text{only with } D_s^{(*)+} D_s^{(*)-}: \Delta\Gamma_s/\Gamma_s = (10.2 \pm 3.0)\% \text{ Phys. Rev. D 84, 074037}$$

▷ Experimental Results

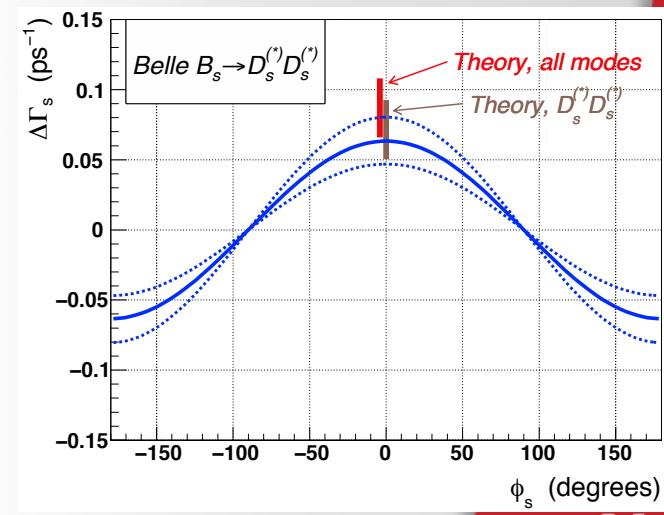
	mode	$\Delta\Gamma_s (\text{ps}^{-1})$	ref.
LHCb	$B_s \rightarrow J/\psi\phi$	$0.123 \pm 0.029 \pm 0.011$	PRL 108 (2012) 101803
ATLAS	$B_s \rightarrow J/\psi\phi$	$0.053 \pm 0.021 \pm 0.008$	arXiv:1208.0572
CDF	$B_s \rightarrow J/\psi\phi$	$0.075 \pm 0.035 \pm 0.006$	PRD 85 (2012) 072002
D0	$B_s \rightarrow J/\psi\phi$	$0.163^{+0.065}_{-0.064}$	PRD 85 (2012) 032006
CDF	$B_s \rightarrow D_s^{(*)+} D_s^{(*)-}$	0.048 ± 0.010	PRD 108 (2012) 201801
Belle	$B_s \rightarrow D_s^{(*)+} D_s^{(*)-}$	0.062 ± 0.016	arXiv:1208.0323

putting back ϕ_s into equation:

$$\frac{\Delta\Gamma_s}{\Gamma_s} = \frac{1/\cos\phi_s - \sqrt{(1/\cos\phi_s)^2 - 4\mathcal{B}(1-\mathcal{B})}}{(1-\mathcal{B})}$$



Dunietz, Fleischer, Nierste, PRD 63, 114015 (2001)
 Chua, Hou, Shen, Phys. Rev. D 84, 074037 (2011)

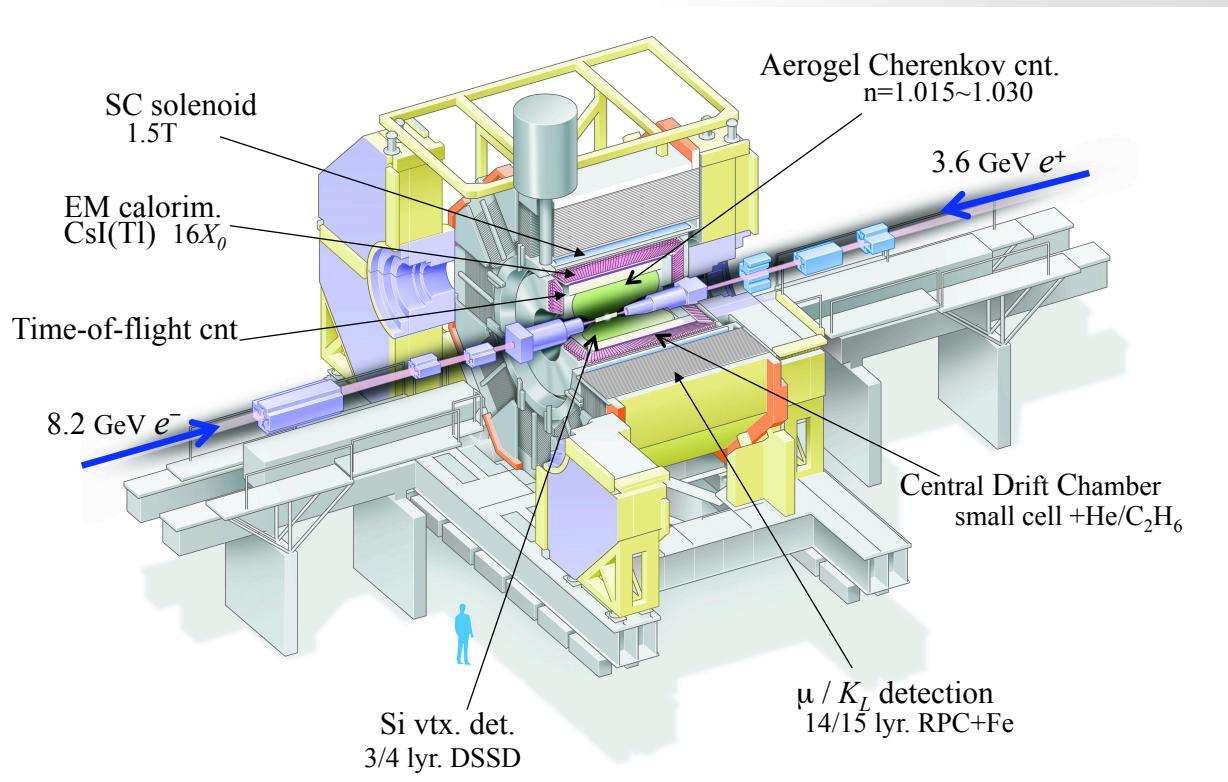


- ▷ Exclusive measurements with 121.4 fb^{-1} data
 - $\mathcal{B}(B_s \rightarrow D_s^+ D_s^-) = 0.58^{+0.11}_{-0.09} \pm 0.13\%$
 - $\mathcal{B}(B_s \rightarrow D_s^{*\pm} D_s^{*\mp}) = 1.8 \pm 0.2 \pm 0.4\%$
 - $\mathcal{B}(B_s \rightarrow D_s^{*+} D_s^{*-}) = 2.0 \pm 0.3 \pm 0.5\%$
 - where sum is $\mathcal{B}(B_s \rightarrow D_s^{(*)+} D_s^{(*)-}) = (4.3 \pm 0.4 \pm 1.0)\%$
 - Good agreement with SM expectation and other measurements.
- ▷ Estimation of $\Delta\Gamma_s/\Gamma_s$, assuming negligible CPV
 - $\Delta\Gamma_s/\Gamma_s = (9.0 \pm 0.9 \pm 2.2)\%$
 - Theoretical uncertainties:
 - size of 3-body partial widths is unknown, \Rightarrow could be large
 - CP-odd component of $D_s^* D_s^*$ is unknown. \Rightarrow expected to be $\sim 6\%$
- ▷ Results are submitted to PRD, arXiv:1208.0323



Backup

30



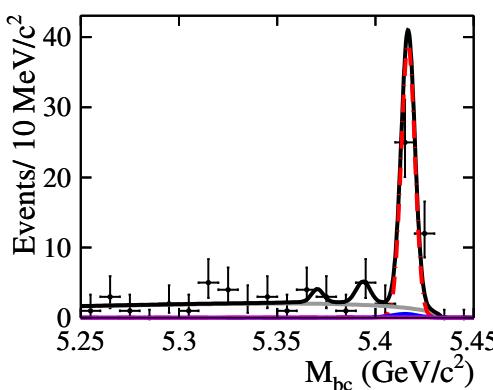
Fully factorized 2D PDF defined for each component (j):

$$\mathcal{P}_j^i = \mathcal{P}_j(\Delta E^i) \mathcal{P}_j(M_{bc}^i)$$

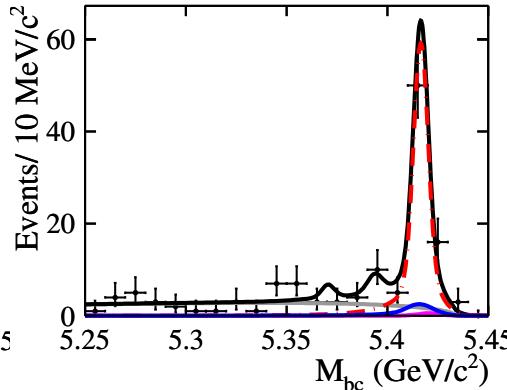
		$D_s^+ D_s^-$	$D_s^{*\pm} D_s^\mp$	$D_s^{*+} D_s^{*-}$
ΔE	\mathcal{RC}		$2\mathcal{G}$ (common mean)	
	\mathcal{WC}	$Cheby + 2\mathcal{G}$	$Cheby + 2\mathcal{G}$	$Cheby + \mathcal{G}$
M_{bc}	\mathcal{RC}		\mathcal{G}	
	\mathcal{WC}		$CBS + \mathcal{G}$	
		$D_s^+ D_s^-$	$D_s^{*\pm} D_s^\mp$	$D_s^{*+} D_s^{*-}$
ΔE	$C\mathcal{F} \rightarrow D_s^+ D_s^-$	-	$Cheby + \mathcal{G}$	$Cheby$
	$C\mathcal{F} \rightarrow D_s^{*\pm} D_s^\mp$	$Cheby + 2\mathcal{G}$	-	$Cheby + \mathcal{G}$
	$C\mathcal{F} \rightarrow D_s^{*+} D_s^{*-}$	$Cheby + \mathcal{G}$	$3\mathcal{G}$	-
M_{bc}	$C\mathcal{F} \rightarrow D_s^+ D_s^-$	-	$CBS + \mathcal{G}$	\mathcal{Novo}
	$C\mathcal{F} \rightarrow D_s^{*\pm} D_s^\mp$	$CBS + \mathcal{G}$	-	$CBS + \mathcal{G}$
	$C\mathcal{F} \rightarrow D_s^{*+} D_s^{*-}$	$\mathcal{Novo} + \mathcal{G}$	$CBS + \mathcal{G}$	

Signal Region Projections

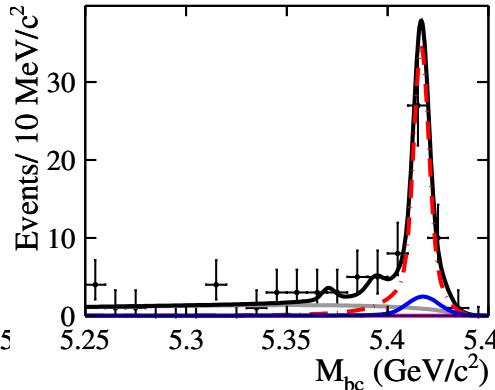
select events in $\Delta E[-0.1, 0.0]$ and $M_{bc}[5.4, 5.43]$



$$D_s^+ D_s^- = 33.1^{+6.0}_{-5.4}$$

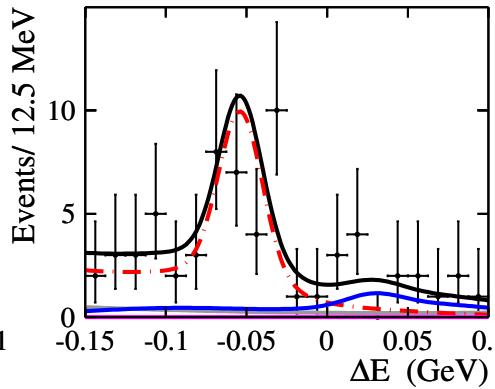
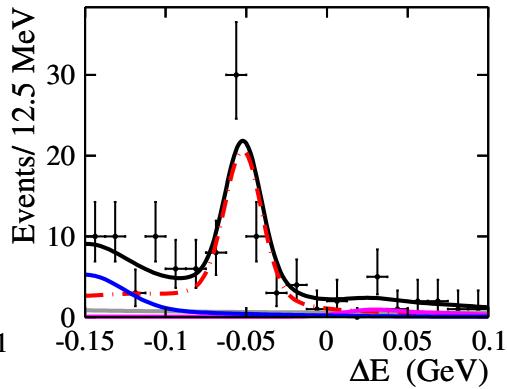
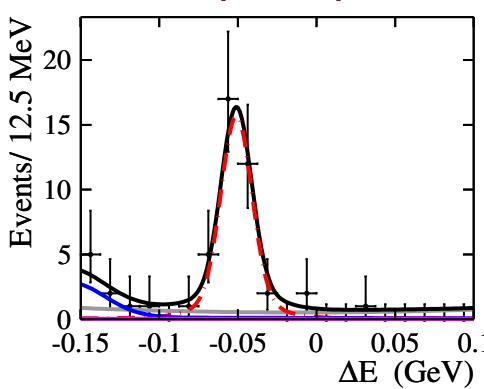


$$D_s^{*+} D_s^- = 44.5^{+5.8}_{-5.5}$$



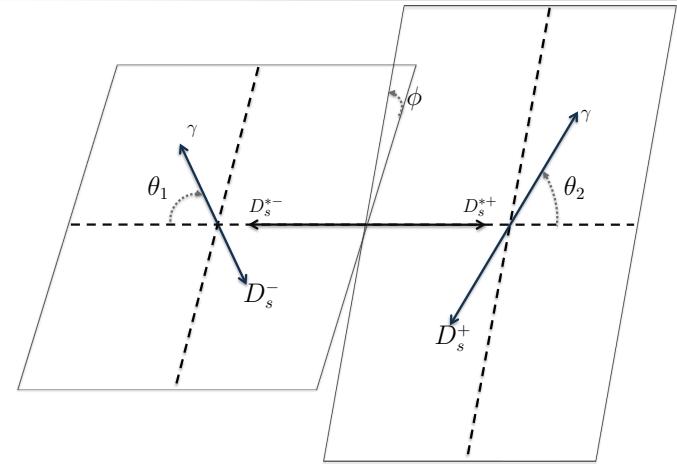
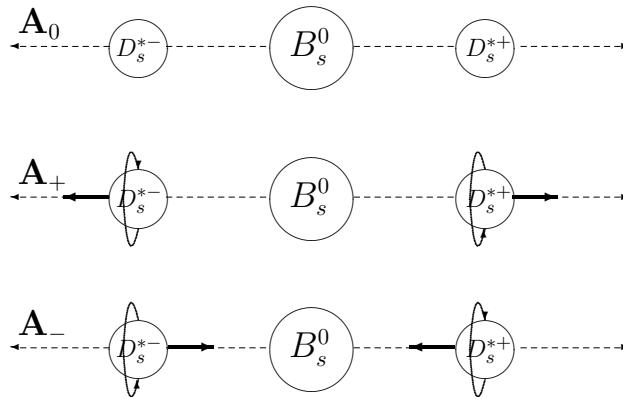
$$D_s^{*+} D_s^{*-} = 24.4^{+4.1}_{-3.8}$$

select events in $M_{bc}[5.4, 5.43]$



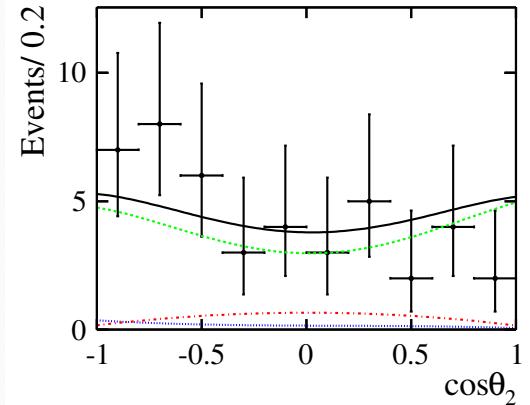
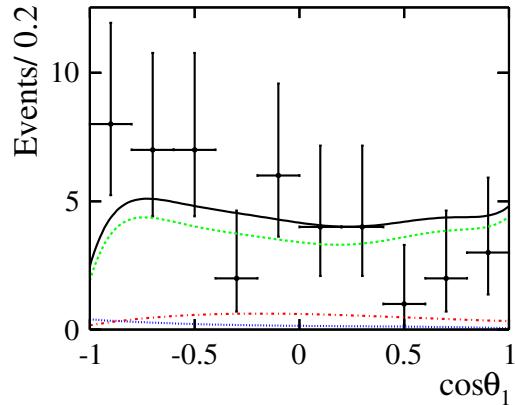
$B_s \rightarrow D_s^{*+} D_s^{*-}$ *Polarization*

- The spin projections along the decay axis must be zero or in opposite directions
- Two helicity and one azimuthal angles
- Integrating over ϕ eliminates the interference terms



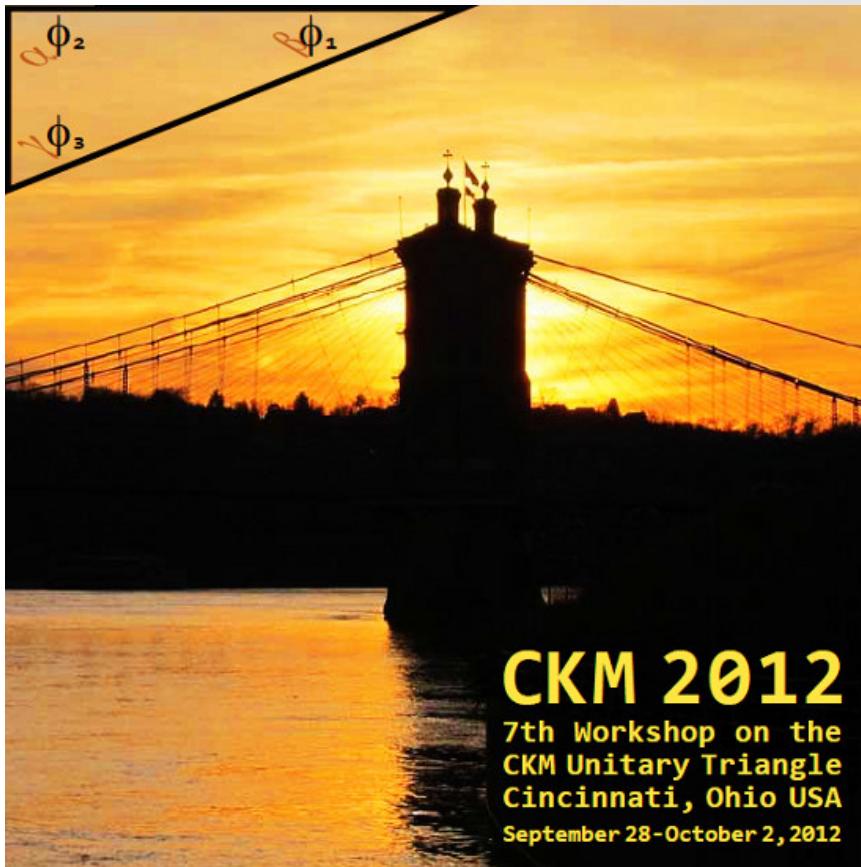
$$\frac{d^2\Gamma(\theta_1, \theta_2)}{d \cos \theta_1 d \cos \theta_2} \propto (|A_+|^2 + |A_-|^2) [(\cos^2 \theta_1 + 1)(\cos^2 \theta_2 + 1)] + |A_0|^2 [4 \sin^2 \theta_1 \sin^2 \theta_2]$$

- ✓ \mathcal{CP} -odd fraction is expected to be $\sim 6\%$ (*J. Rosner, PRD 42, 3732 (1990)*)
- ✓ Longitudinal polarization fraction is expected to be $\sim 50\%$
- ✓ use same cuts as branching fraction measurement
- ✓ select events in 2.5σ signal $M_{bc}\text{-}\Delta E$ region ($B_s^*B_s^*$)
 - almost pure signal: expected background is less than 2 events.
 - expected signal: 45 ± 7 in total
- ✓ two polarization state:
 - A_{\pm} transverse : \mathcal{CP} -odd + \mathcal{CP} -even
 - A_0 longitudinal : \mathcal{CP} -even
- ✓ perform 2D fit in the helicity basis using angles θ_1 and θ_2
- ✓ measure longitudinal fraction $f_L \Rightarrow$ lower bound for \mathcal{CP} -odd?



$$f_L = 0.12^{+0.30+0.04}_{-0.28-0.05}$$

Source	$+\sigma$	$-\sigma$	Method
PDF Shape of \mathcal{RC}	0.0126	0.0111	vary by $\pm\sigma$
PDF Shape of \mathcal{WC}	0.0092	0.0076	vary by $\pm\sigma$
PDF Shape of background	0.0182	0.0181	vary by $\pm\sigma$
Fraction of \mathcal{WC}	0.0092	0.0107	vary by 50%
Fraction of background	0.0280	0.0276	vary by 100%
Continuum Supp.	0	0.0272	fit with no cut
MC efficiency	0.0009	0.0004	vary by $\pm\sigma$
Sum	0.0380	0.0461	



<http://ckm2012.uc.edu/>